Aspectual Caml: an Aspect-Oriented Functional Language *

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Abstract

We propose an aspect-oriented programming (AOP) language
called *Aspectual Caml* based on a strongly-typed functional lan-
guage Objective Caml with two AOP mechanisms similar to those
in AspectJ language. This paper describes the design and imple-
mentation issues of those AOP mechanisms that give us insights
into the interaction between AOP features and common features in
strongly-typed functional languages such as type inference, poly-
morphic types and curried functions. We implemented a prototype
compiler of the language and used the language for separating
crosscutting concerns in application programs, including for sepa-
rating descriptions of a type system from compiler descriptions.

Categories and Subject Descriptors D.3.2 [*Language Classifica-
tions*]: Applicative (functional) languages; D.3.3 [*Language Con-
structs and Features*]: Data types and structures, Modules, pack-
ages, Polymorphism

General Terms Languages

Keywords Aspect-oriented programming, Objective Caml, point-
cut and advice.

1. Introduction

Aspect-Oriented Programming (AOP)[10, 19] is a programming
paradigm for modularizing *crosscutting concerns*, which can not
be well modularized with existing module mechanisms. Several
research and industrial projects have proven the usefulness of
AOP for modularizing crosscutting concerns such as enforcement
of error-handling, optimizations, and authentication in large-scale
software systems including operating systems and commercial ap-
plication servers[5, 6, 7]. Although AOP is claimed to be useful
to programming languages with module mechanisms, it has been
mostly studied in the contexts of object-oriented programming lan-
guages such as Java[3, 4, 17, 18], C++[24], and Smalltalk[9, 16].

In this paper, we propose an AOP language called *Aspectual
Caml* based on a functional language Objective Caml. The goal of
development of Aspectual Caml is twofold. First, we aim to assist
development of practical functional programs with AOP. Even with

sophisticated module systems of functional languages, it would not
be easy to modularize concerns like debugging, logging, optimiza-
tions and security. We believe AOP mechanisms equally useful to
those kinds of concerns in functional languages. Second, we aim
to provide Aspectual Caml as a basis of further theoretical stud-
ies on AOP features. Strongly-typed functional languages, such as
ML and Haskell, offer many powerful language features based on
solid theoretical foundations. Aspectual Caml, which incorporates
existing AOP language features into a strongly-typed functional
language, would help theoretical examination of the features.

Aspectual Caml is an AOP extension to Objective Caml, a
dialect of ML functional language. We design its AOP features by
adapting the AOP features in AspectJ, including the pointcut and
advice mechanism and the inter-type declaration mechanism, for a
functional language with polymorphic types and type inference. We
also design the AOP features so that they would fit key properties of
strongly-typed functional programming including type safety, type
inference, and curried functions.

The language is implemented as a translator to Objective Caml
by extending the parser and type checker of the Objective Caml
compiler.

The rest of the paper is organized as follows. Section 2 intro-
duces the AOP features of Aspectual Caml. Section 3 presents our
current implementation. Section 4 shows case studies of modular-
ization of crosscutting concerns in some application programs with
Aspectual Caml. Section 5 discusses related work. Section 6 con-
cludes the paper.

2. AOP Mechanisms in Aspectual Caml

This section describes the language design of Aspectual Caml.
First we briefly introduce basic notions of AOP. We then overview
problems of introducing AOP features into functional languages
and solutions to those problems. Next, we present an example
of extending a small program (which is called a *base program*
in this paper) with an aspect. We then discuss the design of the
AOP features, namely the pointcut and advice mechanism and the
type extension mechanism with emphases on the differences from
AspectJ.

2.1 Static and Dynamic AOP Mechanisms

An AOP language has one or more language mechanisms for mod-
ularizing crosscutting concerns. Each mechanism can be explained
by using a *join point model*[19, 21], in which the *join points* are the
set of elements that can be treated by the mechanism.

A typical AOP language has two AOP mechanisms: one is for
dynamic program behavior, and the other is for static program
structure. For example, AspectJ has the pointcut and advice mecha-
nism and the inter-type declarations mechanism. The former mech-
anism employs points in program execution, such as method calls
and field accesses, as join points so that aspects can modify the

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dynamic behavior. The latter mechanism employs elements of program structure, such as classes, methods and fields, as join points so that aspects can change class hierarchy.

Aspectual Caml also has two AOP mechanisms, namely the pointcut and advice mechanism and the type extension mechanism. This is because we found that the combinations of two AOP mechanisms are crucial in many practical AOP programs, and found no reason to discard one in functional programming.

2.2 Design Issues

Although the AOP features of Aspectual Caml are similar to the ones in AspectJ, designing those features was not a trivial task. Unique features in the base language (*i.e.,* Objective Caml), compared from Java, such as higher-order functions, variant types (also known as algebraic types), and polymorphic types, require reconsideration of most AOP features.

Below, we briefly discuss some of the notable issues in the design of AOP features in Aspectual Caml, and our proposed solutions:

Type inference: ML (including Objective Caml) and Haskell programs usually omit types in expressions thanks to the type inference system, whereas types are more explicitly written in Java and AspectJ program. Aspectual Caml has a type inference system for pointcut and advice descriptions.

Polymorphic types: Strongly typed languages such as ML and Haskell often have polymorphic types. We found that polymorphic types in pointcuts sometimes break programmers' intuition. This is coped with two types of pointcuts, namely *polymorphic* and *monomorphic* pointcuts.

Curried functions: Functional programs often use curried functions to receive more than one parameters. If the semantics of `call` pointcut were merely capture one application to functions, it would be inconvenient to identify second or later applications to curried functions. To cope with this problem, Aspectual Caml offers *curried pointcuts*.

Static AOP mechanism: Although AOP mechanism similar to the inter-type declarations in AspectJ would be useful, they should be carefully designed because functional programs usually represent structured data by using variant types, whereas object-oriented programs do by using classes. In particular, the inter-type declarations in AspectJ relies on the type compatibility of classes with additional instance variables and methods, which is not guaranteed for the variant types. The type extension mechanism in Aspectual Caml therefore has limited scope to preserve type compatibility.

2.3 Example: Extending Simple Interpreter

This section shows a program with an aspect to give an overview of the AOP mechanisms in Aspectual Caml. The base program is an interpreter of a simple language written in Objective Caml. The simple language merely has numbers, variables, additions and let-terms. The aspect adds a new kind of terms—subtractions—into the simple language without directly changing original interpreter definitions.

2.3.1 Simple Language Interpreter

The interpreter definition begins with definitions for variables which are of type `id`, an identifier type:

```
type id = I of string
let get_name (I s) = s
```

A term is of variant type `t`, which can vary over number (`Num`), variable (`Var`), addition (`Add`), and let (`Let`) terms:

```
type t = Num of int
```

```
aspect AddSubtraction
  type+ t = ... | Sub of t * t
  pointcut evaluation env t = call eval env; t
  advice eval_sub = [around evaluation env t]
    match t with
    Sub(t1, t2) -> (eval env t1) - (eval env t2)
  | _ -> proceed t
end
```

Figure 1. An aspect that adds subtraction to interpreter

```
      | Var of id
      | Add of t * t
      | Let of id * t * t
```

There are a couple of functions and a variable for manipulating environments, whose definitions are omitted here:

```
let extend = (* env -> id -> int -> env *)
let lookup = (* id -> env -> int *)
let empty_env = (* env *)
```

The interpreter `eval` is a recursive function that takes an environment and a term and returns its value:

```
let rec eval env t = match t with
| Num(n) -> n
| Var(id) -> lookup id env
| Add(t1, t2) ->
    let e = eval env in (e t1) + (e t2)
| Let(id, t1, t2)  ->
    eval (extend env id (eval env t1)) t2
```

For example, the following expression represents evaluation of `let x=3+4 in x+x`, which yields 14.

```
eval empty_env (Let(I("x"), Add(Num(3),Num(4)),
                Add(Var(I("x")),Var(I("x")))))
```

2.3.2 Adding Subtraction to the Simple Language

Figure 1 shows an aspect definition in Aspectual Caml that extends the interpreter to support subtractions. The first line declares the beginning of an aspect named `AddSubtraction`, which spans until keyword `end`. The body of the aspect consists of an extension to the data structure and a modification to the evaluation behavior.

The second line is *type extension* that adds an additional constructor `Sub` to type `t` so that extended interpreter can handle subtraction terms. Within `AddSubtraction` aspect, the type `t` has a constructor `Sub` as well as other constructors defined in the base program. Section 2.5 explains this mechanism in detail.

The third line defines a pointcut named `evaluation` that specifies any application of an environment and a term to `eval` function. The pointcut also binds variables `env` and `t` to the parameters of `eval`. This is also an example of *curried pointcut* that can specify applications to curried functions. Section 2.4.2 will explain this in detail.

Lines 4–7 are an advice declaration named `eval_sub` that evaluates subtraction terms augmented above. The keyword `around` on the right hand side at the fourth line specifies that the body of the advice runs instead of a function application matching the pointcut `evaluation`. The lines 5–7 are the body of the advice, which subtracts values of two sub-terms when the term is a `Sub` constructor. Otherwise, it lets the original `eval` interpret the term by applying the term to a special variable `proceed`, which is bound to a function that represents the rest of the computation at the function application.

Note that the pointcut and the body of the advice have no type descriptions, which is similar to other function definitions

Table 1. Kinds of Join Points in Aspectual Caml and AspectJ

in Aspectual Caml	in AspectJ
function call	method call
function execution	method execution
construction of a variant	constructor call
pattern matching	field get

Table 2. Summary of Primitive Pointcuts

syntax	matching join points
`call` N P_1 `;` `...;` P_n	function call
`exec` N P_1 `;` `...;` P_n	function execution
`new` $N(P_1,...,P_n)$	construction of a variant
`match` P	pattern matching (before selecting a variant)
`within` N	all join points within a static scope specified N

in Objective Caml. The type system infers appropriate types and guarantees type safety of the program.

2.4 Pointcut and Advice Mechanism

Aspectual Caml offers a pointcut and advice mechanism for modularizing crosscutting program behavior. The following three key elements explains the mechanism:

- *join points* are the points in program execution whose behavior can be augmented or altered by advice declarations.
- *pointcuts* are the means of identifying join points, and
- *advice declarations* are the means of effecting join points.

The design is basically similar to those in AspectJ-like AOP languages. We mainly explain the notable differences below.

2.4.1 Join Points

Similar to AspectJ-like languages, Aspectual Caml has a dynamic AOP mechanism, in which join points are the points in program execution, rather than the points in a program text. There are four kinds of join points in Aspectual Caml, which are listed in Table 1 with their AspectJ counterparts. Those join points are conservatively selected by considering those in AspectJ and hypothetical aspect definitions written for Objective Caml programs. Although there are variety of additional kinds of join points, such as construction of function closures and access to reference cells, we believe that further experience of writing aspects in Aspectual Caml would give us a better insight into an appropriate set of join points.

Note that the correspondences between Aspectual Caml and AspectJ are rather subjective as functional programs and Java-like object-oriented programs often express similar concepts in different ways. For example, functional programs often use variant types to represent compound data while object-oriented programs use objects. Therefore we place the pattern matching (which takes field values out of a variant) and field get join points in the same row. There are no field-set-like join points in Aspectual Caml since values of variant types are immutable[1].

A join point holds properties of program execution, such as the name of the function to be applied to and values and types of arguments. The names of functions are those directly appear in program text. For example, evaluation of `let lookup = List.assoc in lookup var env` generates a function call join point whose function name is `lookup`, rather than `List.assoc`. We believe that programmers give meaningful names to functions even if the higher-order functions make renaming of functions quite easy in functional programming [2].

We distinguish functional call and execution join points, similar to AspectJ's method call and execution join points. The distinction would be useful for coping with aliasing in functional

programming. A call join point represents application to a function at caller's side, which might use aliased name (e.g., `lookup` for `List.assoc` in the above example). On the other hand, an execution join point represents evaluation of a function body at callee's side, which contains an original name of the function (e.g., `List.assoc` in the above example).

A pattern matching join point represents an operation to access a value of type a variant record regardless superficial syntax in a program. Even when a `match with` expression with many cases (i.e., pairs of a pattern and an expression), it creates only one join point. Therefore, there is no direct means to advise in the middle of pattern matching. Future work would relax this limitation, but we have not encountered examples that require precise control over the order of pattern matching thus far.

Note that function call join points include those to anonymous functions such as `(fun x -> x+1) 3`.

2.4.2 Pointcuts

A pointcut is a predicate over join points. It tests join points based on the kinds and properties of join points, and binds values in the join point to variables when matches.

Primitive Pointcuts: Similar to AspectJ, Aspectual Caml has a sublanguage to describe pointcuts. Table 2 lists the syntax of primitive pointcuts and kinds of join points selected by respective pointcuts. In the table, N denotes a name pattern and P_i denotes a parameter pattern.

A name pattern N is a string of alphabets, numbers, and wildcards followed by a type expression. It matches any function or constructor whose name matches the former part, and whose type matches the latter part. When `call` or `exec` pointcuts use a wildcard in a name pattern N, they match calls or executions of any function including an anonymous function. The type expression can be omitted for matching functions of any type.

A parameter pattern P is a pattern that used to describe a formal parameter of a function in Objective Caml[3]. It is either a variable name, or a constructor with parameter patterns, followed by a type expression. It matches any value of the specified type, or any value that is constructed with the specified constructor and the field values that match respective the parameter patterns. Again, the type expression can be omitted. For example, "`x:int`" matches any integer. "`Add(Num(x),Var(y))`" matches any `Add` term whose first and second fields are any `Num` and `Var` terms, respectively. Note that parameter patterns with constructors are basically runtime conditions. This is similar to `args`, `this` and `target` pointcuts in AspectJ which can specify runtime types of parameters.

Pointcut `within`(N) matches any join point that is created by an expression appearing in a lexical element (e.g., a function definition) matching N. In order to specify function definitions nested in other function definitions, the pattern N can use a path expression, which is not explained in the paper.

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[1] Many functional programming languages offer *references* for representing mutable data. The operations over references are also the candidates of join points in future version of Aspectual Caml.

[2] In contrast, models of AOP languages should be tolerant with renaming of variables. MiniAML [26], for example, distinguishes between variable names and signatures that pointcuts match by introducing labels into the calculus.

[3] In Objective Caml, it is simply called a "pattern", but we refer it to as a "parameter pattern" for distinguishing from the name patterns.

Table 3. Summary of Combined Pointcuts

syntax	matches join points when
C_1 or C_2	either C_1 or C_2 matches
C_1 and C_2	both C_1 and C_2 match
not C	C does not match
cflow C	C or cflowbelow C match
cflowbelow C	there exists a calling-context matching C
I_0 I_1 $\ldots I_n$	named pointcut I_0 matches

Parameter Binding: The parameter patterns in a primitive pointcut also bind parameters to variables. For example, when string `"abc"` is applied to function `lookup` and there is a pointcut `call lookup name`, the pointcut matches the join point and binds the string `"abc"` to the variable `name` so that the advice body can access to the parameter values. When a pattern has an underscore character ("`_`") instead of a variable name, it ignores the parameter value.

Combining and Reusing Pointcuts: As summarized in Table 3, Aspectual Caml offers various means of combining and reusing pointcuts similar to AspectJ. In the table, C denotes a pointcut and I denotes pointcut name or variable name. There are the operators for combining pointcuts, namely `and`, `or`, `not`, and `cflow`. It also supports named pointcuts. For example, the line 3 in Figure 1 names a pointcut expression (`call eval env; t`) `evaluation`,

```
pointcut evaluation env t = call eval env; t
```

which can be used in a similar manner to primitive pointcuts in the subsequent pointcut expressions, like `evaluation env t` at line 4 in the same figure.

Pointcuts for Curried Functions: The `call` and `exec` pointcuts also support curried functions. For example, `call eval env; t` matches the second partial application to function `eval`. Therefore, when an expression `eval empty_env (Num 0)` is evaluated, the pointcut matches the application of (`Num 0`) to the function returned by the evaluation of `eval empty_env`. The pointcut matches even when the partially applied function is not immediately applied. As a result, when `let e = eval env in (e t1) + (e t2)` is evaluated, the applications of `t1` and `t2` to `e` match the above call pointcut.

The following definition gives more precise meaning to `call` pointcuts:

- `call` N P_1 matches evaluation of an expression (e_0 e_1) when the expression e_0 matches the name pattern N and the expression e_1 matches the parameter pattern P_1.
- `call` N P_1; $\ldots$; P_n matches evaluation of an expression (e_0 e_1) when the evaluated value of e_0 is returned from a join point matching `call` N P_1; $\ldots$; $P_{(n-1)}$ and the expression e_1 matches the parameter pattern P_N.

In the above example, since the evaluation of `eval env` matches `call env` and `e` binds its evaluated value, evaluations of (`e t1`) and (`e t2`) match `call eval env; t`.

Similarly, `exec` pointcuts support curried functions on the callee's side.

Section 3.4 presents how this advice declarations with a curried pointcut can be implemented.

Type Inference for Pointcuts: When types are omitted in a pointcut expression, they are automatically inferred from the advice body in which the pointcut is used. This fits with the programming style in Objective Caml, where types can be omitted as much as possible.

For example, the advice `eval_sub` in Figure 1 has no type expressions in the pointcut `evaluation env t`. However, it is inferred from the expressions in the advice body, that the types of the variables `env` and `t` and the return type of the function are the types `env`, `t` and `int`, respectively. As a result, the pointcut, whose definition is `call eval env; t`, matches applications to a function named `eval` and of type `env` $\rightarrow$ `t` $\rightarrow$ `int`.

The type inference gives the most general types to the variables in the pointcuts. In the following advice definition, the system gives fresh type variables α and β to variables `env` and `t`, respectively:

```
advice tracing = [around call eval env; t]
  let result = proceed t in print_int result; result
```

As a result, the pointcut matches any applications to functions whose type is more specific than $\alpha \rightarrow \beta \rightarrow$ `int`. As a result, this advice captures applications to `eval` as well as other `eval` functions that takes two parameters and returns integer values.

Polymorphic and Monomorphic Pointcuts: Aspectual Caml provides a mechanism that programmers can make the types in a named pointcut either polymorphic or monomorphic. This is useful when there are more than one advice definition that uses the same named pointcut. When a named pointcut is defined with the keyword `concrete`, it is a *monomorphic pointcut* whose type variables can not be further instantiated. Otherwise, it is a *polymorphic pointcut* whose type variables are instantiated when the pointcut is used in an advice definition[4].

For example, the `evaluation` pointcut in Figure 1 is polymorphic. It hence matches any function applications `eval` of type $\forall \alpha \beta \gamma . \alpha \rightarrow \beta \rightarrow \gamma$. When `evaluation` used in advice `eval_sub`, the type system instantiates α, β, and γ and then infers the types with respect to the advice body. Therefore, another advice definition that uses `evaluation` with different types do not conflict with the previous advice definition:

```
advice tracing = [before evaluation env t]
  print_string env; print_string t
```

This mechanism is quite similar to the let-polymorphism in ML languages.

Although the polymorphic pointcuts are useful to define generalized pointcuts, they are sometimes inconvenient when the programmer wants to specify the same set of join points at any advice that uses the same pointcut. *Monomorphic pointcuts* are useful in such a situation. Consider the following aspect definition that prints messages at the beginning and end of any function application (Note that `??$` is a wildcard that matches any name):

```
aspect Logging
  pointcut logged n = call ??$ n
  advice log_entry = [before logged n]
    print_string ("\nenters with "^(string_of_int n))
  advice log_exit = [after logged n]
    print_string "\nexits"
end
```

Since `logged` is a polymorphic pointcut that matches any application to functions of type $\forall \alpha \beta . \alpha \rightarrow \beta$, the type system instantiates type variables for each advice declaration. Hence the first advice matches only functions that take integer values as their parameter, whereas the second matches any function.

By declaring `logged` pointcut with the keyword `concrete` and type expression to the variables that are used in the advice:

---

[4] Note that polymorphic pointcuts instantiate type variables only when types are omitted in the pointcut descriptions. It is possible to give concrete types to some parameters in a pointcut, while leaving other parameters polymorphic.

```
concrete pointcut logged n = call ??$ (n:int)
```

`logged` pointcut becomes monomorphic that matches any application to functions of type $int \rightarrow \alpha$. With this pointcut definition, the two advice definitions are guaranteed to advise the same set of join points because the types in the pointcut will not be instantiated further.

2.4.3 Advice

An advice definition includes the name, timing keyword, pointcut, and body expression. The timing keyword, either `around`, `before`, and `after`, specifies that the advice body runs instead of, before or after each join point matching the pointcut. In the body of advice, the programmer can use all top-level variables, variables bound by the pointcut, and the special function `proceed` (available only in `around` advice). Since `proceed` means the original behavior, it resumes the original execution when it is applied with an argument.

For preserving type safety, the body expression of `around` advice must have the same type as returning values of specified join points. In addition, that of `before` and `after` advice must have the type `unit`. In the example of subtraction extension, the body of `eval_sub` has the type `int` that is the same type as a result value of `eval`.

2.5 Type Extension Mechanism

The type extension mechanism allows aspects to define extra fields or constructors in variant types (also known as algebraic types) in a base program. The former mechanism can be seen as a rough equivalent to the inter-type instance variable declarations in AspectJ.

Despite the simplicity of the mechanism, we believe that it is as crucial as the pointcut and advice mechanism. As you can observe in example programs in AspectJ, not a few crosscutting concerns contain not only behavior (which is implemented by the pointcut advice mechanism) but also data structures (which are implemented by the inter-type declarations).

2.5.1 Defining Extra Constructs

One of the abilities of the type extension mechanism is to define additional constructors to existing variant types. A variant type definition `type+` T `= ... |` C adds constructor C to existing type whose type name is T. In Figure 1, we have already seen an example that adds `Sub` constructor to the type `t`.

The constructors added to a variant type by aspects often make pattern matching non-exhaustive. In other words, a base program that originally defined the variant type usually has functions that process for each constructor differently (*e.g.*, `eval` in the simple interpreter). Therefore, an aspect that added a constructor to a variant type would also need to advise such functions so as to process the case for the additional constructor. In the example Figure 1, the advice `eval_sub` processes the constructor `Sub` for the function `eval`, which otherwise reports non-exhaustiveness warnings.

2.5.2 Defining Extra Fields

The type extension mechanism can also allow to define additional fields to constructors of existing variant types. A variant type definition

$$\texttt{type+}\ T_0 = C\ \texttt{of}\ ...\ *\ T_1\{e_1\}\ *\ \cdots\ *\ T_n\{e_n\}$$

adds fields of type $T_1, \ldots, T_n$ to a constructor C of type T_0. The expressions $e_1, \ldots, e_n$ in the curly brackets specify default values to the respective fields.

For example, assume we want to associate a number (*e.g.*, a line number in a source program) to each variable in the simple language of Section 2.3. A solution with the type extension mecha-

nism is to add an integer field to `ident` type by writing the following definition:

```
type+ ident = I of ... * int{0}
```

As the base program originally defines `ident` type as `type ident = I of string`, a value created by the constructor `I` has a pair of string and integer.

The extended fields are visible only in the aspects that define the extension. This means that a value of the extended type looks differently inside and outside of the aspect:

- Inside the same aspect, the extended type is seen with the extended fields. Therefore, `I ("x",1)` is a correct expression in the aspect.
- Outside the aspect, although values of the extended type have extended fields, the extended fields are hidden. Therefore, a value created by `I ("x",1)` inside the aspect is seen as `I "x"` outside the aspect. Conversely, evaluation of `I "y"` outside the aspect uses the default value `0` for the value of the extended field, which actually yields `I ("y",0)` when viewed from inside the aspect.

3. Implementation

We implemented a compiler, or a weaver of Aspectual Caml as a translator to Objective Caml. Many parts of the compiler are implemented by modifying internal data structures and functions in an Objective Caml compiler as the AOP features deeply involve with the type system.

The compiler first parses a given program to build a parse tree. Then the next five steps process the parse tree:

1. infers types in the base function definitions;
2. infers types in the aspect definitions;
3. modifies variant type definitions in the base program by processing type extensions;
4. simplify advice definitions; and
5. inserts applications to advice bodies into matching expressions.

Finally, it generates Objective Caml program by unparsing the modified parse tree.

Below, those five steps are explained by using the example in Section 2.3.

3.1 Type Inference for Base Functions

The types in the base function definitions are inferred by using the internal functions in the original Objective Caml compiler. After the type inference, all variables in the functions are annotated with types (or type schemes):

```
type id = I of string
let (get_name:id->string) = fun (I(s:string)) -> s
type t =          (* omitted *)
let extend =      (* ibid. *)
let lookup =      (* ibid. *)
let empty_env = (* ibid. *)
let rec (eval:env->t->int) =
  fun (env:env) -> fun (t:t) -> match t with
| Num(n:int) -> n
| Var(id:id) -> lookup id env
| Add((t1:t), (t2:t)) ->
    let (e:t)->int = eval env in (e t1) + (e t2)
| Let((id:id), (t1:t), (t2:t))  ->
    eval (extend env id (eval env t1)) t2
```

3.2 Type Inference for Aspects

The types in aspect definitions are inferred in a similar manner to the type inference for the base functions. Notable points are the treatments of polymorphic/monomorphic pointcuts, and scope of the variables.

The type of a pointcut is a type of join points that can match the pointcut and a type environment for the variables in the pointcut. The type of matching join points is decided by the shapes of primitive pointcuts in the pointcut and the types of the variables. The variables bound by the pointcuts have unique type variables otherwise explicitly specified. For polymorphic pointcuts, those type variables are quantified with universal quantifiers that can be instantiated at the advice definitions. Monomorphic pointcuts use the special type variables that can not be instantiated in the later processes.

For example, evaluation pointcut in Figure 1 has, type of $\forall \alpha\beta\gamma.\alpha \rightarrow \beta \rightarrow \gamma$ for the matching join points with a type environment env : β, t : γ for variables bound by the pointcut.

Note that the type inference of pointcuts does not use the types of function names; *e.g.,* the type of eval in the base program. This is because the function names in pointcuts do not necessarily refer to specific functions in the base program, but they rather refer to any function that have matching name.

The type inference of an advice definition is basically similar to the type inference of a function definition, but it takes types of parameters from the types of the pointcut, and gives a type to proceed variable that is implicitly available in the advice body. Given an advice definition advice a = [around call p] e where p is a pointcut of join point type $\alpha_1 \rightarrow \cdots \rightarrow \alpha_n \rightarrow \beta$ and type environment Γ, the type of e is inferred under the global type environment extended with Γ, proceed : $\alpha_n \rightarrow \beta$.

For example, type inference of eval_sub advice uses a global type environment extended with env : α, t : β, proceed : $\beta \rightarrow \gamma$, and assigns types as follows:

```
(* global type environment has
   Sub:t*t->t, eval:env->t->int *)
advice eval_sub
 = [around evaluation (env:env) (t:t)]
   (* let proceed:t->int *)
   match t with
     Sub((t1:t), (t2:t)) ->
       (eval env t1) - (eval env t2)
   | _ -> proceed t
```

Note that the types of eval and Sub are taken from the global type environment, which eventually instantiates the types of other variables including those in the pointcut.

3.3 Reflect Type Modifications in Base Programs

In this phase, type extensions are reflected in the base programs. The definition of types are changed according to the aspects. Additionally, the default values are added to expressions whose fields are extended by the aspects.

3.4 Simplify Advice Definitions

The next step is to transform the advice definitions into simpler ones in order to make the later weaving process easier.

First, it transforms every before and after advice definition into around advice, by simply inserting an application to proceed at the beginning or end of the advice body.

Second, it transforms an advice declaration that uses curried pointcuts so that all call or exec pointcuts takes exactly one parameter. The next is a translated advice definition from eval_-sub (inferred types are omitted for readability):

```
advice eval_sub = [around call eval env]
   let proceed = proceed env in
     fun t -> match t with
         Sub(t1, t2) -> (eval env t1) - (eval env t2)
       | _ -> proceed t
```

When an environment is applied to eval, the transformed advice runs and returns a function that runs the body of the original advice when it takes a term. In other words, eval is advised to return a function that runs the original advice body.

Generally, it transforms an advice definition with a curried pointcut by iteratively removing the last parameter in the curried pointcut by using the following rule that transforms an advice definition:

```
advice a = [around call f v₁; ···; vₙ]
   e
```

into the next one:

```
advice a = [around call f v₁; ···; vₙ₋₁]
   let proceed = proceed vₙ₋₁ in
     fun vₙ -> e
```

There is a subtle problem with this approach when curried pointcuts are used with a disjunctive (or) operator, which is left for future research. The problem is a conflict with advice execution policy in AspectJ-like languages. In AspectJ, an advice definition runs at most once for each (dynamic) join point. In other words, when there is an advice definition that prints a message, and a program calls a function, the advice should print only one message. In Aspectual Caml, the following advice definition with curried pointcut causes the problem:

```
advice trace_eval_or_e =
   [around (call eval _; t) || (call e t)]
   print_string "eval"; proceed t
```

When we evaluate eval empty_env (Add(Num(0), Num(1))) with this advice, evaluation of each subexpression of Add is advised twice if the advice declaration is translated by following the above rule. This is because the advice is translated into the following two advice declarations:

```
advice trace_eval_or_e_1 = [around (call eval env)]
   let proceed = proceed env in
   fun t -> print_string "eval"; proceed t
advice trace_eval_or_e_2 = [around (call e t)]
   print_string "eval"; proceed t
```

Since eval has a subexpression let e = eval env in (e t1) + (e t2), the first advice modifies the value of e to run the body of the advice, and the second advice runs the body of the advice at e t1 and e t2, respectively. Consequently, evaluation of e t1 and e t2 runs the body of advice twice.

3.5 Weave Advice Definitions

The last step is to insert expressions that runs advice bodies at appropriate times in the base functions. It first transforms each advice definition into a function definition. It then walks through all expressions (*i.e., join point shadows*) in the function definitions, and inserts an application to an advice function when it matches the pointcut of the advice.

Given an advice definition, the first step is to simply generate a recursive function that takes proceed parameter followed by the parameters to the advice. For example, it generates the following function for eval_sub advice (again, types are omitted for readability):

```
let rec eval_sub proceed env =
```

```
    let proceed = proceed env in
      fun t -> match t with
          Sub(t1, t2) -> (eval env t1) - (eval env t2)
        | _ -> proceed t
```

The second step is to rewrite the bodies of the base functions[5] so that they call advice functions at appropriate places. By traversing the expressions in the given program, for each expression type of function application, lambda abstraction, constructor application, or pattern matching for structured values, it looks for advice definitions that have the respective kind of primitive pointcuts. When the name pattern of the pointcut matches the name in the expression, and the type of the pointcut is more general than the type of the expression, it replaces the expression with an application to the advice function.

For example, `eval` function in the base program has a sub-expression `(eval env)` where `eval:env->t->int` and `env:env`. This application sub-expression matches the `call` pointcut in `eval_sub` as the types of the join point and the pointcut are the same. In this case, it replaces the expression with `(⟨eval_sub⟩ eval env)` where `⟨eval_sub⟩` is an expression that references the advice function (explained below).

It is a little tricky to define and reference advice functions due to recursiveness introduced by advice. An advice definition has a global scope; it can advise any execution in any module and it also can use global functions defined in any module. Consequently, advice definitions can introduce recursion into non-recursive functions in the original program. For example, the following code fragment recursively computes factorial numbers by advising the non-recursive function `fact`[1]:

```
let fact n = 1
aspect Fact
  advice realize = [around exec fact n]
    if n=0 then proceed n else n*(fact (n-1))
end
```

In order to allow advice to introduce recursion, we proposed two solutions:

- Define advice functions in a *recursive module*[20] in Objective Caml. As recursive modules allow mutual recursion between functions across modules, this would directly solve the problem.

- Reference advice functions via mutable cells. In this solution, the translated program begins with definitions of mutable cells that hold advice functions. The subsequent function definitions run advice functions by dereferencing from those mutable cells. Finally, after defined advice functions, the program stores the advice functions into the mutable cells.

Although trickier, our current implementation uses the latter solution. We will consider the former one in our future version.

After finished above processes, the compiler generates the following translated code for the example program:

```
(* define mutable cells for advice functions *)
let eval_sub_ref = ref (fun _ -> failwith "")
(* definitions for id, t and env are omitted *)
let rec eval env t = match t with
| Num(n) -> n
| Var(id) -> lookup id env
| Add(t1, t2) ->
    let e = !eval_sub_ref eval env in
    (e t1) + (e t2)
```

```
| Let(id, t1, t2)  ->
    !eval_sub_ref
    eval
    (extend env id (!eval_sub_ref eval env t1))
    t2
(* advice function *)
let rec eval_sub proceed env =
  let proceed = proceed env in
  fun t -> match t with
      Sub(t1, t2) ->
        (!eval_sub_ref eval env t1) -
        (!eval_sub_ref eval env t2)
    | _ -> proceed t
(* store advice function into mutable cell *)
let _ = eval_sub_ref := eval_sub
```

Note that all applications to `eval` function, including those in the advice body, are replaced with applications to `!eval_sub_-ref eval`. The `eval_sub_ref` is defined at the beginning of the program with a dummy value, and assigned `eval_sub` function at the end of the program.

3.6 Implementation Status

Thus far, we developed a prototype implementation[6] of Aspectual Caml. Although some of the features discussed in the paper are not available yet, it supports essential features for validating our concept, including the type extension, around advice, and most kinds of primitive pointcuts except for wildcarding. In fact, the next section introduces an example that can be compiled by our prototype implementation.

The current implementation has approximately 24,000 lines of Objective Caml program (of which 2,000 lines are modified or added for implementing Aspectual Caml), including the parser and type inference system that are modified from the ones in the original Objective Caml compiler. Although it would be theoretically possible to directly pass the translated parse tree to the back-end Objective Caml compiler, our compiler generates source-level program by unparsing the parse tree. This is mainly for the ease of development and for debugging.

4. Application Programs

Among several small application programs that we have written in Aspectual Caml, we briefly sketch two of them.

The one is, as we have seen thought the paper, to augment an interpreter of a simple language with additional kinds of terms, such as subtraction. Although it is a very small program, the aspect illustrates its usefulness for pluggable extension; since the aspect does not require to change the original interpreter definitions, we can easily fall back to the original language.

The second application program is larger. It extends a compiler of an untyped language to support static type system. The base part of the program define types for the parse trees of the source and intermediate languages and functions that translate the parse tree in the source language into the intermediate language called K-normal forms. The aspects extend the type of the source parse tree with type information, and modifies the transformation functions to carry out type inference during the transformation.

The aspects in the program can improve comprehensibility of the compiler implementation in particular educational purposes. Since the translation rules in the original can be complicated by the types, separating the compiler into the one for untyped language

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[5] Precisely, the base functions also include the advice bodies. This enables to advise execution of advice as well as execution of function.

[6] Available at `http://www.graco.c.u-tokyo.ac.jp/ppp/projects/acaml/`.

and the extension for types would clarify both the core translation rules and the interaction between translations and type system.

The second program, which consists of approximately 100 lines of base program and 100 lines of aspect definitions, is shown in Appendix A.

5. Related Work

AspectJ[17, 18] is the first AOP language that offers both the pointcut and advice and inter-type declaration mechanisms. Aspectual Caml is principally designed by following those mechanisms. However, we see AspectJ-family of languages might be too complicated to theoretically study the AOP features as they primarily aim practical languages. For example, AspectJ 1.2 compiler does not report type errors for the following advice declaration:

```
Object around() : call(Integer *.*(..))
{ return new Float(0); }
```

even though it could cause a runtime error if applied to an expression like `Integer.decode("0").intValue()`. A simpler language that yet has a notion of polymorphism would help to reason about such a situation.

There are several proposals of theoretical models of AOP features. As far as the authors know, most work merely on the pointcut and advice mechanism. Aspect SandBox[27] describes a semantics of an dynamically-typed procedural language with a pointcut and advice mechanism. Tucker and Krishnamurthi presented a pointcut and advice mechanism in dynamically-typed functional languages[25]. MiniAML is a core calculus for expressing the pointcut and advice mechanism in strongly-typed functional languages[26]. Such a calculus would be suitable to describe the language design of Aspectual Caml, which is currently explained at the source language level. TinyAspect is a model of pointcut and advice mechanism for strongly-typed languages with ML-like modules[1]. It proposes a module system for aspects so as to protect join points in a module from aspects outside the module.

From the application programmers' viewpoint, Aspectual Caml has several unique language features that can not be found in those theoretical models, including polymorphism in pointcuts and advice, various kinds of pointcuts other than function calls, and the type extension mechanism. On the other hand, those models are theoretically sound; i.e., they come with static and dynamic semantics with proven type soundness. Those properties of Aspectual Caml are to be shown in future.

AspectML is an AOP extension to Standard ML with the pointcut and advice mechanism[26]. The semantics of AspectML is defined as a translation into MiniAML. PolyAML is a polymorphic aspect-oriented functional language[8]. While both Aspectual Caml and PolyAML provide polymorphism in pointcuts and advice declarations, there are several differences in the other AOP features:

- PolyAML has a formal type system that has been proven sound.

- Pointcuts in PolyAML are first-class data, which can be considered generalized mechanism of named pointcuts in Aspectual Caml and other AspectJ-like languages.

- PolyAML can reify calling-contexts so that the programmer can change advice behavior by examining into the context information. This powerful mechanism could be used for `cflow` pointcuts in AspectJ. However, it is not clear how efficient implementation techniques[15, 22] and optimizations based on static analysis[2, 23] can be applied with this mechanism.

- PolyAML provides `case-advice` mechanism that runs advice declarations based on runtime types of parameters, which is essential for defining universal aspects like tracing. Aspectual Caml does not offer mechanisms to examine runtime types

yet. We believe such a feature should be carefully designed in strongly-typed languages like Objective Caml in which types of values are not always available at runtime for efficiency reasons.

- PolyAML pointcuts specify join points by names in scope; i.e., a pointcut `{f}:(t1,t2)` specifies function `f` in the lexical scope in which the pointcut declared, and types `t1` and `t2` are merely used for type checking. It is not clear how PolyAML can advise anonymous functions and locally defined functions without invasively inserting advice declarations into original function definitions. Pointcuts in Aspectual Caml are different in that they match join points in all scope, they can use wildcards for function names, and they can use types for matching. For example, a pointcut `call ??f$ (x:int)` in Aspectual Caml matches any function calls when the name of the function begins with `f` and the type of the first parameter is `int`, even if the functions are defined locally.

- In addition to above differences, Aspectual Caml provides several unique features that are not available in PolyAML, such as support for curried functions and variant types (both in terms of static extension and dynamic advising). We presume those features would also be useful in PolyAML.

There are several studies for adding fields or constructors into existing types, but not in the context of aspect-oriented programming. Type-safe update programming provides a means of extending existing data types[11], which inspired the type extension mechanism in Aspectual Caml. Polymorphic variants[13] allow to define functions that manipulate variant records without prior declaration of the variant type. This can improve code re-usability of a program when it uses polymorphic variants instead of ordinary variants[14]. Since there have been many programs that developed with ordinary variants, we believe that the polymorphic variants and our type extension mechanism would complement each other.

6. Conclusion

This paper presented the design and implementation of Aspectual Caml, an AOP functional language. The language design aims at developing practical applications by adapting many AOP features in existing AOP languages. In order to fit for the programming styles in strongly-typed functional languages, we reconsidered AOP features, including type inference of aspects, polymorphism in pointcuts, and type extension mechanisms. We believe that those features would serve a good basis for further theoretical development of AOP features such as type safety.

A compiler of an Aspectual Caml subset is implemented as a translator to Objective Caml. It is capable to compile non-trivial application programs in which base and aspect definitions deeply interact. Those application programs would also demonstrate that AOP is as useful in functional programming as in object-oriented programming.

We plan to work more on the design and implementation of Aspectual Caml. We so far informally defined the language semantics and compilation processes, which should be defined more formally. A module system for aspects that would nicely work with the ML module system would be investigated. We also consider further polymorphism in advice bodies so as to easily define type universal aspects like tracing. One idea is to integrate the language with G'Caml[12] so that advice can use functions that can examine values in different types.

Yonezawa's research group, the members of PoPL meeting, and the members of Kumiki meeting at University Tokyo for helpful discussion. We thank the anonymous reviewers of an earlier versions of the paper for their helpful comments.

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A. An Example of Compiler written in Aspectual Caml

A.1 Base Program: A Simple Compiler

```
(*type of (untyped) identifiers*)
type ident = I of string

(*type of immediate values*)
type imm =
  | Int of int
  | Float of float
(*terms in the source language*)
type syntax =
  | S_Let of ident * syntax * syntax
  | S_Var of ident
  | S_LetRec of s_fundef list * syntax
  | S_App of syntax * syntax list
  | S_NegInt of syntax
  | S_SubInt of syntax * syntax
  | S_IfLEInt of syntax * syntax * syntax * syntax
  | S_Imm of imm
(*mutually recursive functions*)
and s_fundef = { s_name : ident;
                 s_args : ident list;
                 s_body : syntax }

(*target: untyped K-normal terms*)
type knormal =
  | K_Let of ident * knormal * knormal
```

```
    | K_Var of ident
    | K_LetRec of k_fundef list * knormal
    | K_App of ident * ident list
    | K_NegInt of ident
    | K_SubInt of ident * ident
    | K_IfLEInt of ident * ident * knormal * knormal
    | K_Imm of imm
and k_fundef = { k_name : ident;
                 k_args : ident list;
                 k_body : knormal }

(*return a fresh identifier*)
let fresh_knormal =
  let r = ref 0 in
    fun () -> (incr r; I(("_knormal_" ^
                          (string_of_int !r))))

(*K normalizing for the constructor LetRec*)
let rec knormal_letrec fundef = match fundef with
    [] -> []
  | {s_name = ident;
     s_args = ident_list;
     s_body = exp}::tl ->
      {k_name = ident;
       k_args = ident_list;
       k_body = (knormal exp)}
      ::(knormal_letrec tl)

(*K normalizing for the constructor App*)
and knormal_app exp explist =
  let rec arg_knormal fresh_fun explist id_list =
    let rec sub el il = match el with
        [] -> K_App(fresh_fun, il)
      | exp::tl -> begin match knormal exp with
          K_Var(x) -> sub tl (il@[x])
        | kexp ->
            let fresh_arg = fresh_knormal () in
              K_Let(fresh_arg, kexp,
                    sub tl (il@[fresh_arg]))
        end in
      sub explist id_list in
    insert_let (knormal exp)
               (fun x -> arg_knormal x explist [])

(*K normalizing*)
and knormal = function
    S_Var(x) -> K_Var(x)
  | S_NegInt(exp) ->
      let f x = K_NegInt(x) in
      insert_let (knormal exp) f
  | S_SubInt(exp1, exp2) ->
      insert_let
        (knormal exp1)
        (fun x -> insert_let
                    (knormal exp2)
                    (fun y -> K_SubInt(x, y)))
  | S_IfLEInt(exp1, exp2, exp3, exp4) ->
      insert_let
        (knormal exp1)
        (fun x -> insert_let
                    (knormal exp2)
                    (fun y ->
                        K_IfLEInt(x, y,
                                  knormal exp3,
                                  knormal exp4)))
```

```
  | S_Let(ident, exp1, exp2) ->
      K_Let(ident, knormal exp1, knormal exp2)
  | S_LetRec(fl, exp) ->
      K_LetRec(knormal_letrec fl, knormal exp)
  | S_App(exp, explist) -> knormal_app exp explist
  | S_Imm(i) -> K_Imm(i)

and insert_let e c = match e with
    K_Var(x) -> c x
  | exp -> let fresh = fresh_knormal () in
      K_Let(fresh, exp, c fresh)

(*K normalizing main*)
let knormal_main s_exp = knormal s_exp
```

A.2 An Aspect to Add Typing

```
aspect AddType
(*a type of an expression*)
type typ =
    Tint
  | Tfloat
  | Tvar of typ option ref
  | Tfun of typ list * typ

(*type extension to indentifiers. NOTE: the     *)
(*extended field can only be seen in this aspect*)
type+ ident = I of ... * typ{Tvar(ref None)}

(*return fresh variables with types*)
let fresh_knormal_with_type =
  let r = ref 0 in
    fun typ ->
      (incr r;
       I(("_knormal_" ^ (string_of_int !r)), typ))

(*find concrete type by resolving Tvars*)
let rec get_type = function
    Tvar({contents = Some(t)}) -> get_type t
  | Tfun(t_list, t) ->
      Tfun(List.map get_type t_list, get_type t)
  | t -> t

(*occur check*)
let rec occur r1 = function
    Tint | Tfloat -> false
  | Tfun(t2s, t2') ->
      List.exists (occur r1) t2s || occur r1 t2'
  | Tvar(r2) when r1 == r2 -> true
  | Tvar({ contents = None }) -> false
  | Tvar({ contents = Some(t2) }) -> occur r1 t2

(*unification of two types*)
exception Unify of typ * typ

let rec unify t1 t2 =
  match t1, t2 with
    Tint, Tint | Tfloat, Tfloat -> ()
  | Tfun(t1s, t1'), Tfun(t2s, t2') ->
      (try List.iter2 unify t1s t2s
       with Invalid_argument("List.iter2") ->
         raise (Unify(t1, t2)));
      unify t1' t2'
  | Tvar(r1), Tvar(r2) when r1 == r2 -> ()
  | Tvar({contents = Some(t1')}), _ ->
      unify t1' t2
```

```
  | _, Tvar({contents = Some(t2')}) ->
    unify t1 t2'
  | Tvar({ contents = None } as r1), _ ->
    if occur r1 t2 then raise (Unify(t1, t2));
    r1 := Some(t2)
  | _, Tvar({ contents = None } as r2) ->
    if occur r2 t1 then raise (Unify(t1, t2));
    r2 := Some(t1)
  | _, _ -> raise (Unify(t1, t2))

(*typing expressions after K normalization  *)
(*NOTE: this function uses the extended type*)
(*field in identifiers                      *)
let rec id_typing k_exp t_env = match k_exp with
    K_Var(I(x, typ)) -> begin try
      let typ1 = List.assoc x t_env in
        unify typ typ1; typ
    with Not_found ->
      failwith ("unbound_variable: " ^ x) end
  | K_NegInt(I(_, typ)) -> unify typ Tint; typ
  | K_SubInt(I(_, typ1), I(_, typ2)) ->
     unify typ1 Tint; unify typ2 Tint; Tint
  | K_Let(I(name, typ), k_e1, k_e2) ->
      let typ1 = id_typing k_e1 t_env in
        unify typ1 typ;
        id_typing k_e2 ((name, typ1)::t_env)
  | K_LetRec(k_fundef_list, k_e) ->
      let new_t_env = id_typing_letrec
                        k_fundef_list t_env in
        id_typing k_e new_t_env
  | K_App(id, id_list) ->
      id_typing_app id id_list t_env
  | K_IfLEInt(I(_, typ1),I(_, typ2),k_e1,k_e2) ->
      unify typ1 Tint; unify typ2 Tint;
      let ke1_typ = id_typing k_e1 t_env in
      let ke2_typ = id_typing k_e2 t_env in
        unify ke1_typ ke2_typ;
        ke1_typ
  | K_Imm (Int _) -> Tint
  | K_Imm (Float _) -> Tfloat

(*typing LetRec after K normalization*)
and id_typing_letrec k_fundef_list t_env =
  let rec make_tmp_t_env = function
      {k_name = I(fun_name, typ);
       k_args = id_list;
       k_body = _}::tl ->
        let args_type = List.map
                          (fun (I(_, t)) -> t)
                          id_list in
          unify typ (Tfun(args_type,
                          Tvar(ref None)));
          (fun_name, typ)::(make_tmp_t_env tl)
    | [] -> t_env in
  let tmp_t_env = make_tmp_t_env k_fundef_list in
  let rec id_typing_k_fundefs = function
      {k_name = I(_, fun_type);
       k_args = id_list;
       k_body = k_exp}::tl ->
        let new_t_env = (List.map
                          (fun (I(name, typ)) ->
                            name, typ)
                          id_list)@tmp_t_env in
        let args_type = List.map
                          (fun (I(_, t)) -> t)
```

```
                          id_list in
        let exp_type =
            id_typing k_exp new_t_env in
          unify fun_type
                (Tfun(args_type, exp_type));
          id_typing_k_fundefs tl
    | [] -> () in
    id_typing_k_fundefs k_fundef_list;
    tmp_t_env

(*typing App after K normalization*)
and id_typing_app fun_id arg_ids t_env =
  let id_type id = id_typing (K_Var id) t_env in
  let fun_type = id_type fun_id in
  let arg_types = List.map id_type arg_ids in
  let result_type = Tvar(ref None) in
    unify fun_type (Tfun(arg_types, result_type));
    result_type

(*perform typing after K normalization*)
let rec advising =              (*a flag to detect*)
  ref false                     (*top-level calls *)

advice knormal_with_typing =
        [around (call knormal s_exp)]
  if not !advising then     (*top call to knormal*)
    let _ = advising := true in
    let k_exp = proceed s_exp in
    let _ = id_typing k_exp [] in
    let _ = advising := false in k_exp
  else
    let k_exp = proceed s_exp in k_exp

end
```